



Ryelands Primary and Nursery School

Mathematics Written Calculations Policy

This policy was developed as part of a consultation process involving pupils, staff, parents and Governors of the school, based on best practice advice (where available) from Lancashire County Council.

The implementation of this policy will be monitored by the Senior Leadership Team and Governing Body.

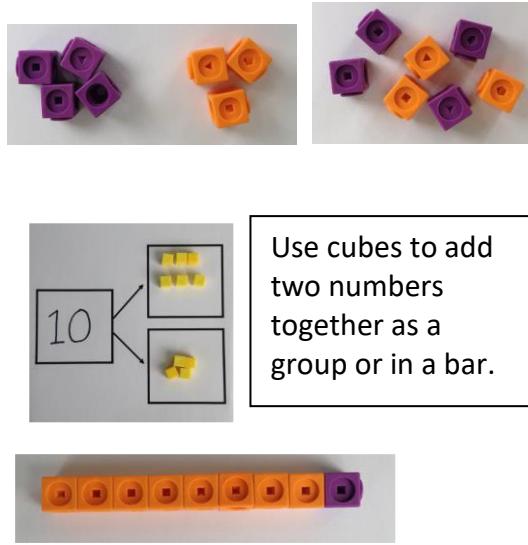
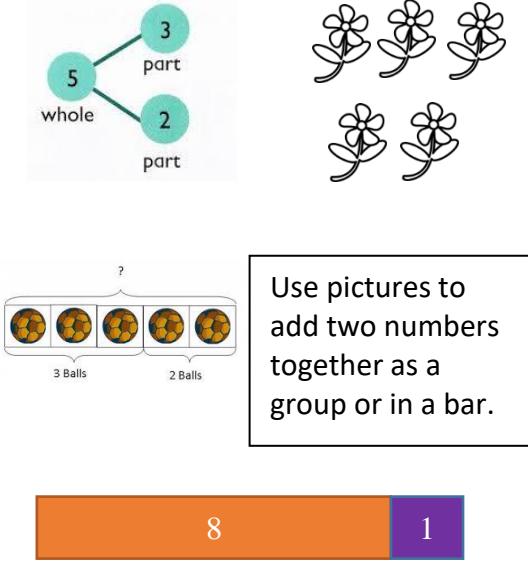
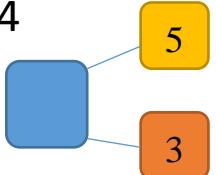
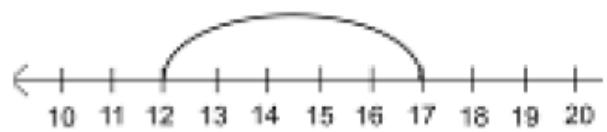
This policy should be read in conjunction with the following documents:

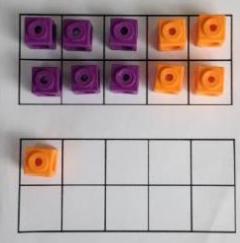
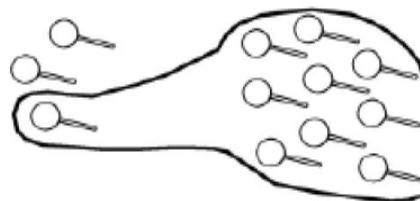
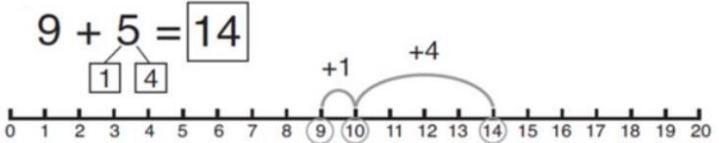
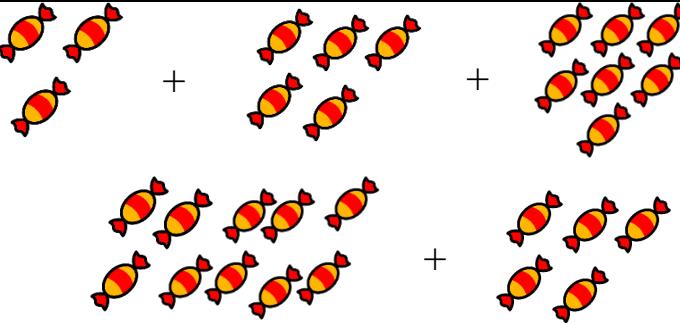
- Teaching and Learning Policy
- Mathematics Policy

| | | | |
|--|--|--|---------------|
| Policy Created: | February 2019 | | |
| First Presented to Governors for approval: | 7 th February 2019 | | |
| Proposed Review Cycle/Next Date: | 3 Year | | February 2028 |
| Approved by (Headteacher) | Approved by (Governor) | | |
| Date: | | Date: | |
| Policy Review History | | | |
| Date: February 2019 | Date: February 2022 | Date: February 2025 | |
| Key Changes: <ul style="list-style-type: none">• Major changes to align approaches with the 'mastery' approach to teaching and learning | Key Changes: <ul style="list-style-type: none">• No changes – date only | Key Changes: No changes – date only | |
| Presented to Governors: Curriculum Committee 7 th February 2019 | Presented to Governors: Curriculum Committee 2 nd February 2022 | Presented to Governors: Curriculum Committee 5 th February 2025 | |

Addition

Key Language: sum, total, parts and wholes, plus, add, altogether, more, 'is equal to' 'is the same as'.

| Objective and Strategies | Concrete | Pictorial | Abstract |
|---|---|--|--|
| Combining two parts to make a whole: part-whole model |  <p>Use cubes to add two numbers together as a group or in a bar.</p> |  <p>Use pictures to add two numbers together as a group or in a bar.</p> | $4 + 3 = 7$ $10 = 6 + 4$  <p>Use the part-part whole diagram as shown above to move into the abstract.</p> |
| Starting at the bigger number and counting on |  <p>Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.</p> | $12 + 5 = 17$  <p>Start at the larger number on the number line and count on in ones or in one jump to find the answer.</p> | $5 + 12 = 17$ <p>Place the larger number in your head and count on the smaller number to find your answer.</p> |

| | | | |
|---|---|---|---|
| <p>Regrouping to make 10.</p> |  <p>$6 + 5 = 11$</p>  <p>Start with the bigger number and use the smaller number to make 10.</p> |  <p>3 + 9 =</p>  | <p>$7 + 4 = 11$</p> <p>If I am at seven, how many more do I need to make 10. How many more do I add on now?</p> |
| <p>Adding three single digits</p> <p>$4 + 7 + 6 = 17$ Put 4 and 6 together to make 10. Add on 7.</p>  <p>Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.</p> | |  <p>Add together three groups of objects. Draw a picture to recombine the groups to make 10.</p> | <p>$4 + 7 + 6 = 10 + 7$ $= 17$</p> <p>Combine the two numbers that make 10 and then add on the remainder.</p> |

| | | | |
|--|---|--|--|
| <p>Column method- no regrouping</p> | <p>$24 + 15 =$ Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.</p> | <p>After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.</p> | <p><u>Calculations</u></p> $ \begin{array}{r} 21 + 42 = \\ 21 \\ + 42 \end{array} $ |
| <p>Column method- regrouping</p> | <p>Make both numbers on a place value grid.</p> <p>Add up the units and exchange 10 ones for one 10.</p> <p>Add up the rest of the columns, exchanging the 10 counters from one</p> | <p>Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.</p> | <p>Start by partitioning the numbers before moving on to clearly show the exchange below the addition.</p> $ \begin{array}{r} 20 + 5 \\ 40 + 8 \\ \hline 60 + 13 = 73 \end{array} $ $ \begin{array}{r} 536 \\ + 85 \\ \hline 621 \end{array} $ |

column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.

As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.

72.8

+ 54.6

127.4

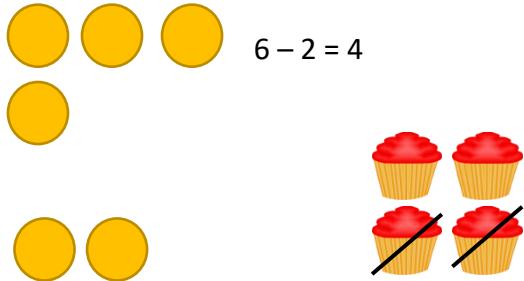
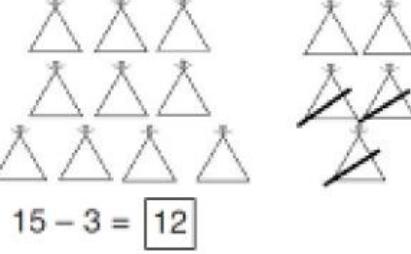
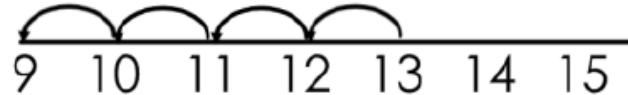
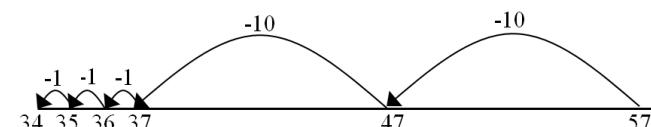
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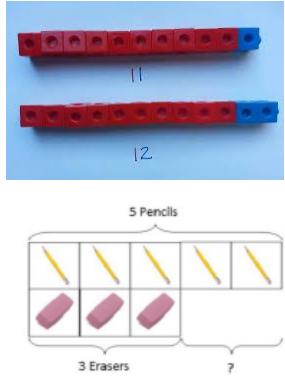
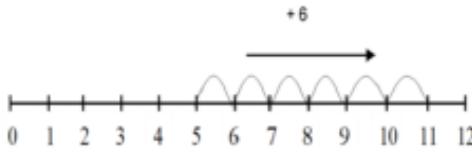
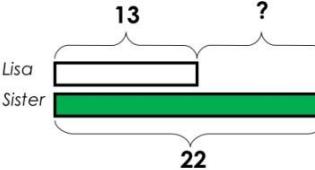
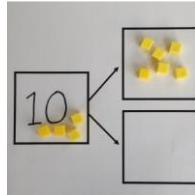
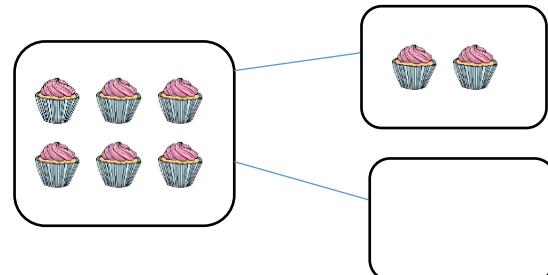
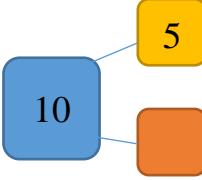
$$\begin{array}{r} \pounds \ 2 \ 3 \ . \ 5 \\ + \pounds \ 7 \ . \ 5 \\ \hline \pounds \ 3 \ 1 \ . \ 1 \\ \hline 1 \ 1 \ 1 \end{array}$$

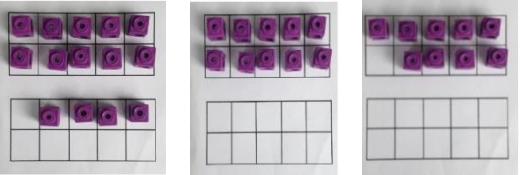
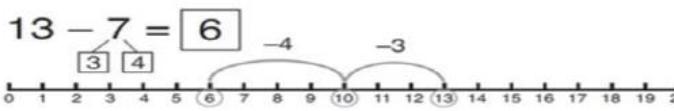
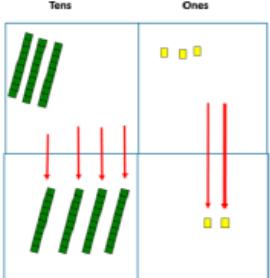
$$\begin{array}{r} 2 \ 3 \ . \ 3 \ 6 \ 1 \\ 9 \ . \ 0 \ 8 \ 0 \\ 5 \ 9 \ . \ 7 \ 7 \ 0 \\ + \ 1 \ . \ 3 \ 0 \ 0 \\ \hline 9 \ 3 \ . \ 5 \ 1 \ 1 \\ \hline 2 \ 1 \ 2 \end{array}$$

Subtraction

Key language: take away, less than, the difference, subtract, minus, fewer, decrease.

| Objective and Strategies | Concrete | Pictorial | Abstract |
|--------------------------|--|---|---|
| Taking away ones | <p>Use physical objects, counters, cubes etc to show how objects can be taken away.</p>  $6 - 2 = 4$  $15 - 3 = 12$ | <p>Cross out drawn objects to show what has been taken away.</p> | $18 - 3 = 15$ $8 - 2 = 6$ |
| Counting back | <p>Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.</p>  $13 - 4$ <p>Use counters and move them away from the group as you take them away counting backwards as you go.</p>  | <p>Count back on a number line or number track</p>  <p>Start at the bigger number and count back the smaller number showing the jumps on the number line.</p>  <p>This can progress all the way to counting back using two 2 digit numbers.</p> | <p>Put 13 in your head, count back 4. What number are you at? Use your fingers to help.</p> |

| | | | |
|--------------------------------|--|--|---|
| <h3>Find the difference</h3> | <p>Compare amounts and objects to find the difference.</p>  <p>Use cubes to build towers or make bars to find the difference</p> <p>Use basic bar models with items to find the difference</p> |  <p>Count on to find the difference.</p> <p>Comparison Bar Models</p> <p>Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them.</p>  | <p>Hannah has 23 sandwiches; Helen has 15 sandwiches. Find the difference between the number of sandwiches.</p> |
| <h3>Part Part Whole Model</h3> |  <p>Link to addition- use the part whole model to help explain the inverse between addition and subtraction.</p> <p>If 10 is the whole and 6 is one of the parts. What is the other part?</p> $10 - 6 =$ | <p>Use a pictorial representation of objects to show the part part whole model.</p>  |  <p>Move to using numbers within the part whole model.</p> |

| | | | | | | | | | | | | |
|---|---|---|--|---|---|---|--|--|---|---|---|---|
| <h3>Make 10</h3> | <p>$14 - 9 =$</p>  <p>Make 14 on the ten frame. Take away the four first to make 10 and then take away one more so you have taken away 5. You are left with the answer of 9.</p> |  <p>Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.</p> | <p>$16 - 8 =$</p> <p>How many do we take off to reach the next 10?</p> <p>How many do we have left to take off?</p> | | | | | | | | | |
| <h3>Column method without regrouping</h3> |  <p>Show how you partition numbers to subtract. Again make the larger number first.</p> <tr> <td>3</td><td>6</td> </tr> <tr> <td>-</td><td>1</td><td>4</td> </tr> <tr> <td colspan="2"> </td><td>=</td> </tr> <tr> <td>2</td><td>0</td> <td>2</td> </tr> | 3 | 6 | - | 1 | 4 | | | = | 2 | 0 | 2 |
| 3 | 6 | | | | | | | | | | | |
| - | 1 | 4 | | | | | | | | | | |
| | | = | | | | | | | | | | |
| 2 | 0 | 2 | | | | | | | | | | |

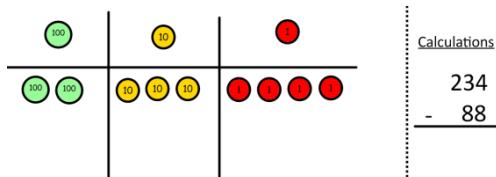
 The ones column shows 6 minus 4 equals 2, and the tens column shows 3 minus 1 equals 2.

 Use Base 10 to make the bigger number then take the smaller number away. Draw the Base 10 or place value counters alongside the written calculation to help to show working. | $$47 - 24 = 23$$ $$\begin{array}{r} 40 + 7 \\ - 20 + 4 \\ \hline 20 + 3 \end{array}$$ This will lead to a clear written column subtraction. |

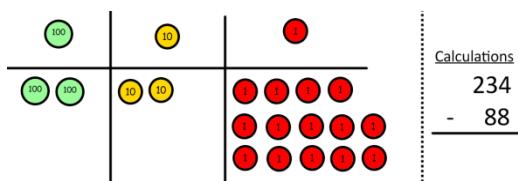
Column method with regrouping

Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

Make the larger number with the place value counters

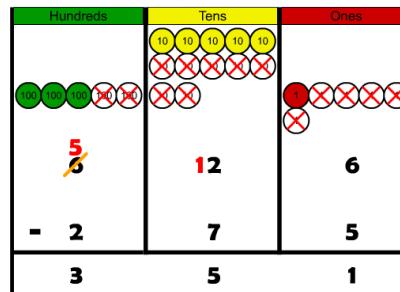


Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.

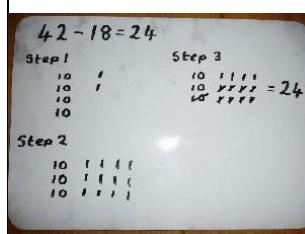


Now I can subtract my ones.

Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.



When confident, children can find their own way to record the exchange/regrouping.

Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup.

$$\begin{array}{r}
 836 - 254 = 582 \\
 \hline
 800 - 200 = 600 \\
 300 - 50 = 250 \\
 600 + 250 = 850 \\
 850 - 80 = 770 \\
 770 - 2 = 768
 \end{array}$$

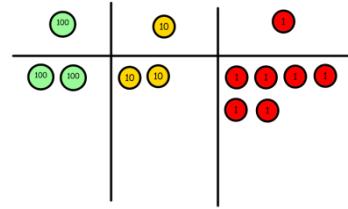
Children can start their formal written method by partitioning the number into clear place value

$$\begin{array}{r}
 728 - 582 = 146 \\
 \hline
 700 - 500 = 200 \\
 20 - 80 = -60 \\
 200 - 60 = 140 \\
 140 + 6 = 146
 \end{array}$$

columns.

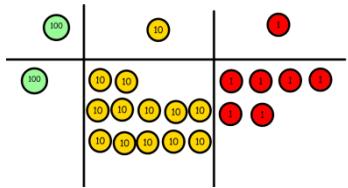
Moving forward the children use a more compact method.

This will lead to an understanding of subtracting any number including decimals.



Calculations

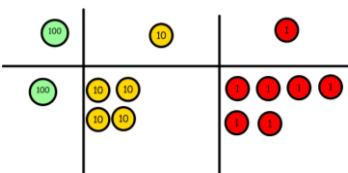
$$\begin{array}{r} 234 \\ - 88 \\ \hline \end{array}$$



Calculations

$$\begin{array}{r} 234 \\ - 88 \\ \hline \end{array}$$

Now I can take away eight tens and complete my subtraction



Calculations

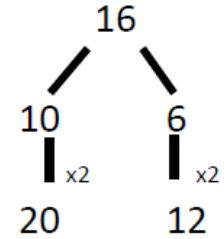
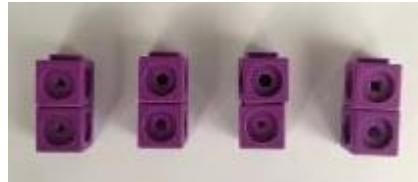
$$\begin{array}{r} 234 \\ - 88 \\ \hline 146 \end{array}$$

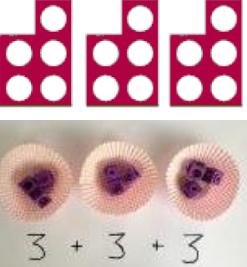
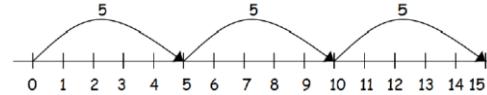
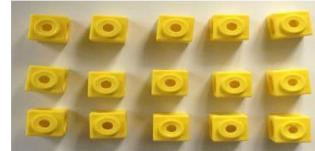
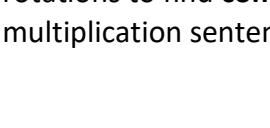
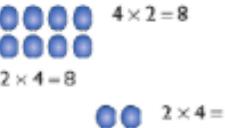
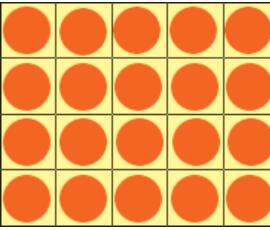
Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.

$$\begin{array}{r} 5121 \\ 2\cancel{6}\cancel{3} \\ \hline 2365 \end{array}$$

Multiplication

Key language: double, times, multiplied by, the product of, groups of, lots of, equal groups

| Objective and Strategies | Concrete | Pictorial | Abstract |
|--------------------------|---|---|--|
| Doubling | <p>Use practical activities to show how to double a number.</p>  <p>double 4 is 8 $4 \times 2 = 8$</p> | <p>Draw pictures to show how to double a number.</p> <p style="text-align: center;">Double 4 is 8</p>  |  <p>Partition a number and then double each part before recombining it back together.</p> |
| Counting in multiples |   <p>Count in multiples supported by concrete objects in equal groups.</p> |   <p>Use a number line or pictures to continue support in counting in multiples.</p> | <p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p> |

| | | | |
|---|--|---|--|
| <h3>Repeated addition</h3> |   <div data-bbox="691 357 925 492"> <p>Use different objects to add equal groups.</p> </div> | <p>There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?</p>  <p>2 add 2 add 2 equals 6</p>  <p>$5 + 5 + 5 = 15$</p> | <p>Write addition sentences to describe objects and pictures.</p>  <p>$2 + 2 + 2 + 2 + 2 = 10$</p> |
| <h3>Arrays- showing commutative multiplication</h3> | <p>Create arrays using counters/ cubes to show multiplication sentences.</p>   | <p>Draw arrays in different rotations to find commutative multiplication sentences.</p>  <p>$4 \times 2 = 8$</p> <p>$2 \times 4 = 8$</p>  <p>$2 \times 4 = 8$</p> <p>$4 \times 2 = 8$</p>  <p>Link arrays to area of rectangles.</p> | <p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p>$5 + 5 + 5 = 15$</p> <p>$3 + 3 + 3 + 3 + 3 = 15$</p> <p>$5 \times 3 = 15$</p> <p>$3 \times 5 = 15$</p> |

Grid Method

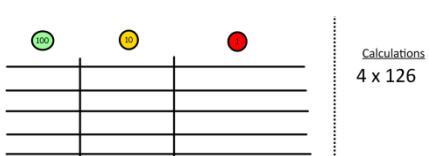
Show the link with arrays to first introduce the grid method.

| | | |
|---|--------------|-------------|
| x | 10 | 3 |
| 4 | 4 rows of 10 | 4 rows of 3 |

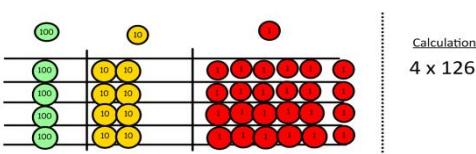
Move on to using Base 10 to move towards a more compact method.

| | | |
|---|--------------|-------------|
| x | T | U |
| | 4 rows of 10 | 4 rows of 3 |

Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.



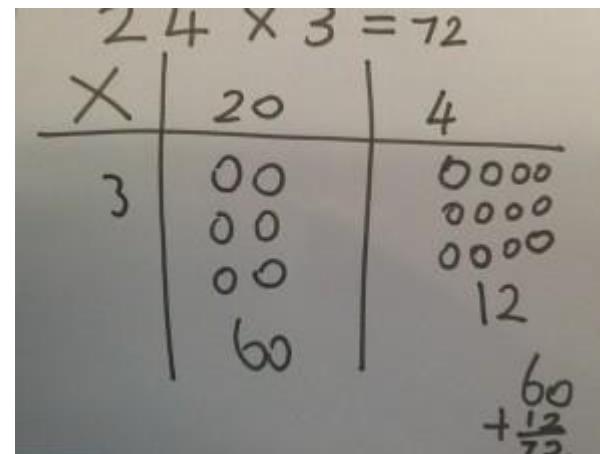
Fill each row with 126.



Add up each column, starting with the ones making any exchanges needed.

Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.



Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

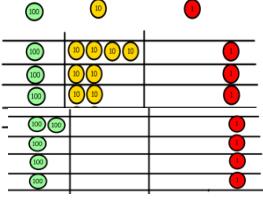
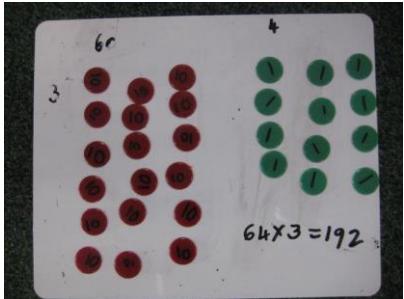
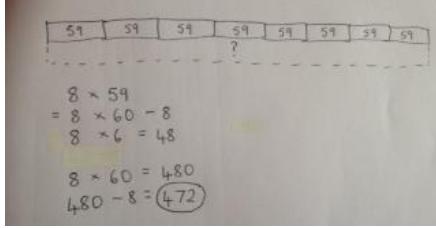
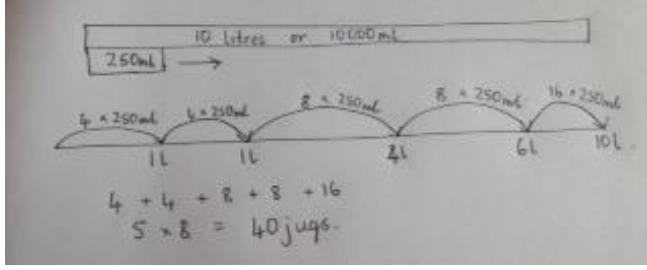
| | | |
|---|-----|----|
| x | 30 | 5 |
| 7 | 210 | 35 |

$$210 + 35 = 245$$

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.

| | |
|----|-----|
| 10 | 8 |
| 10 | 100 |
| 3 | 30 |

| | | | | |
|----|-------|------|-----|----|
| x | 1000 | 300 | 40 | 2 |
| 10 | 10000 | 3000 | 400 | 20 |
| 8 | 8000 | 2400 | 320 | 16 |

| | | | |
|--------------------------------|---|---|---|
| |  <p>Then you have your answer.</p> | | |
| <h3>Column multiplication</h3> | <p>Children can continue to be supported by place value counters at the stage of multiplication.</p>  <p>It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.</p> | <p>Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.</p>   | <p>Start with long multiplication, reminding the children about lining up their numbers clearly in columns.</p> <p>If it helps, children can write out what they are solving next to their answer.</p> $ \begin{array}{r} 32 \\ \times 24 \\ \hline 8 \quad (4 \times 2) \\ 120 \quad (4 \times 30) \\ 40 \quad (20 \times 2) \\ 600 \quad (20 \times 30) \\ \hline 768 \end{array} $ |

$$\begin{array}{r} 7 & 4 \\ \times & 6 & 3 \\ \hline 1 & 2 \\ 2 & 1 & 0 \\ 2 & 4 & 0 \\ + & 4 & 2 & 0 & 0 \\ \hline 4 & 6 & 6 & 2 \end{array}$$

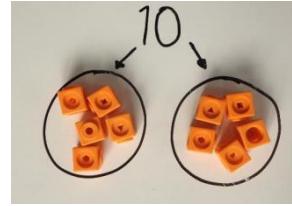
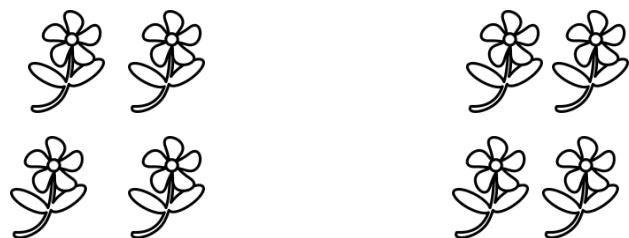
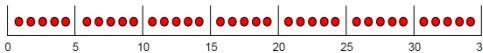
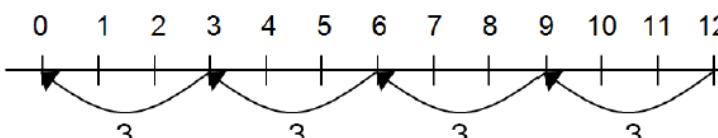
$$\begin{array}{r} 2 & 3 & 1 \\ 1 & 3 & 4 & 2 \end{array}$$

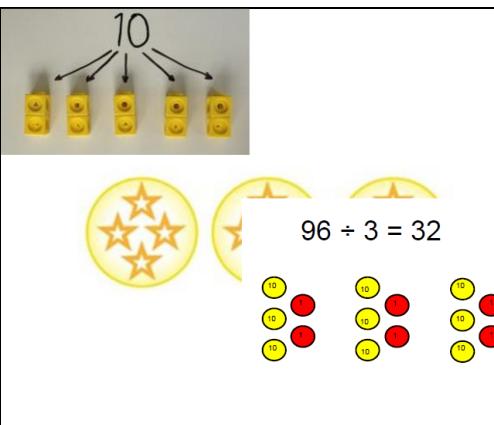
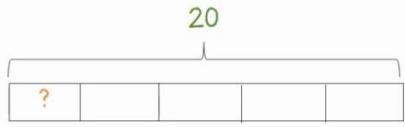
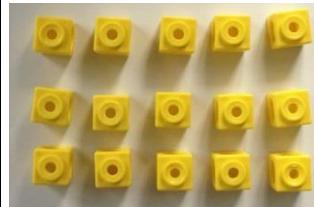
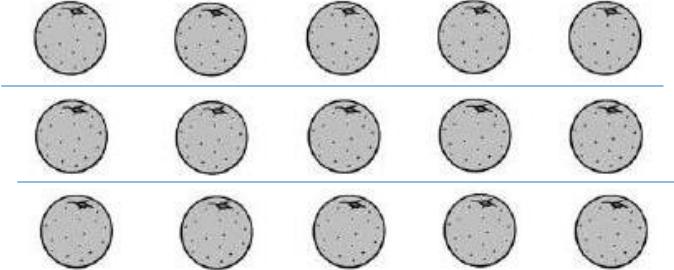
$$\begin{array}{r} x & 18 \\ \hline 1 & 3 & 4 & 2 & 0 \\ 1 & 0 & 7 & 3 & 6 \\ \hline 2 & 4 & 1 & 5 & 6 \\ 1 \end{array}$$

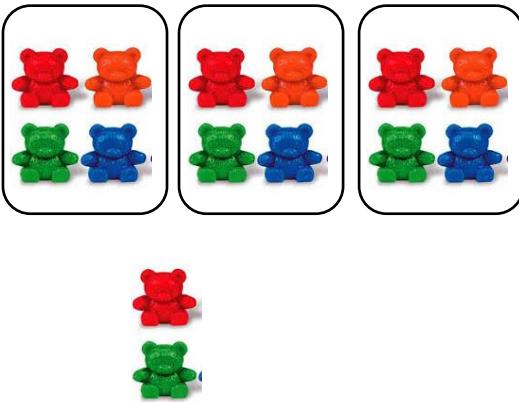
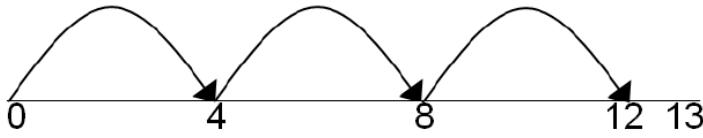
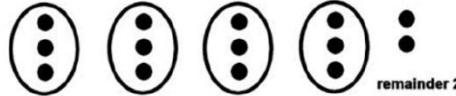
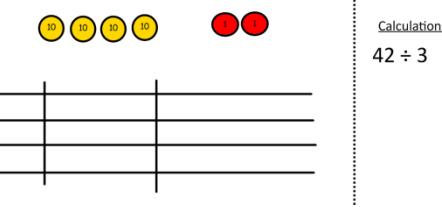
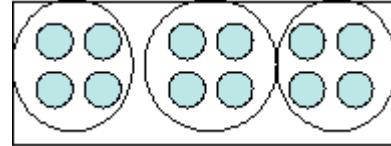
This moves to
the more
compact
method.

Division

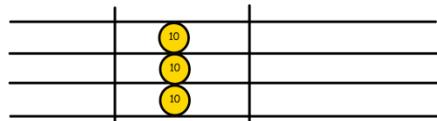
Key language: share, group, divide, divided by, half.

| Objective and Strategies | Concrete | Pictorial | Abstract |
|-----------------------------|---|--|---|
| Sharing objects into groups |  <p>I have 10 cubes, can you share them equally in 2 groups?</p>  | <p>Children use pictures or shapes to share quantities.</p>  <p>$8 \div 2 = 4$</p> | <p>Share 9 buns between three people.</p> $9 \div 3 = 3$ |
| Division as grouping | <p>Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.</p>  | <p>Use a number line to show jumps in groups. The number of jumps equals the number of groups.</p>  | $28 \div 7 = 4$ <p>Divide 28 into 7 groups. How many are in each group?</p> |

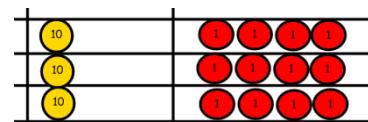
| | | | |
|-------------------------------|---|--|---|
| |  | <p>Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.</p> <p>20</p>  <p>$20 \div 5 = ?$ $5 \times ? = 20$</p> | |
| <p>Division within arrays</p> |  <p>Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p> <p>Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$</p> |  <p>Draw an array and use lines to split the array into groups to make multiplication and division sentences.</p> | <p>Find the inverse of multiplication and division sentences by creating four linking number sentences.</p> <p>$7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$</p> |

| | | | | | | | | | |
|--|--|---|---|---|---|--|--|--|---|
| <h3>Division with a remainder</h3> | <p>$14 \div 3 =$ Divide objects between groups and see how much is left over</p>  | <p>Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.</p>  <p>Draw dots and group them to divide an amount and clearly show a remainder.</p>  | <p>Complete written divisions and show the remainder using r.</p> $29 \div 8 = 3 \text{ REMAINDER } 5$ <p style="text-align: center;">↑ ↑ ↑ ↑</p> <p>dividend divisor quotient remainder</p> | | | | | | |
| <h3>Short division</h3> | <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">Tens</td> <td style="text-align: center;">Units</td> </tr> <tr> <td style="text-align: center;">3</td> <td style="text-align: center;">2</td> </tr> <tr> <td colspan="2" style="text-align: center; border-top: 1px solid black; border-bottom: 1px solid black;">  </td> </tr> </table> <p>Use place value counters to divide using the bus stop method alongside</p>  <p>$42 \div 3 =$</p> | Tens | Units | 3 | 2 |  | | <p>Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.</p>  <p>Encourage them to move towards counting in multiples to divide more efficiently.</p> | <p>Begin with divisions that divide equally with no remainder.</p> $ \begin{array}{r} & 2 & 1 & 8 \\ & \underline{3} & & \\ 4 & 8 & 7 & 2 \end{array} $ |
| Tens | Units | | | | | | | | |
| 3 | 2 | | | | | | | | |
|  | | | | | | | | | |

Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.



We exchange this ten for ten ones and then share the ones equally among the groups.



We look how much in 1 group so the answer is 14.

Move onto divisions with a remainder.

$$\begin{array}{r} 86 \\ 5 \overline{)432} \\ 40 \end{array} \quad r \ 2$$

Finally move into decimal places to divide the total accurately.

$$\begin{array}{r} 14.6 \\ 35 \overline{)511.0} \\ 35 \end{array} \quad 16 \quad 21$$